

or

$$G_{\sigma\mathbf{k}}(\omega_\nu) = \mathcal{G}_{\sigma\mathbf{k}}(\omega_\nu) + \mathcal{G}_{\sigma\mathbf{k}}(\omega_\nu)\Sigma_{\sigma\mathbf{k}}(\omega_\nu)G_{\sigma\mathbf{k}}(\omega_\nu) \quad (2.5)$$

$$= \frac{1}{i\omega_\nu + \mu - t_{\mathbf{k}} - \Sigma_{\sigma\mathbf{k}}(\omega_\nu)}.$$

Here

$$\mathcal{G}_{\sigma\mathbf{k}}(\omega_\nu) = \frac{1}{i\omega_\nu + \mu - t_{\mathbf{k}}} \quad (2.6)$$

and the self-energy $\Sigma_{\sigma\mathbf{k}}(\omega_\nu)$ describes all scattering processes originated from the second term in (2.1) and cannot be divided into parts by cutting off one zero-order Green's function $\mathcal{G}_{\sigma\mathbf{k}}(\omega_\nu)$ line.

Also, it is well known that within such a weak-coupling approach the electron susceptibilities (charge, spin, etc.) can be presented in the form

$$\chi_{\mathbf{q}}^{AB}(\omega_m) = - \text{diagram} + \text{diagram with } D, \quad (2.7)$$

where the type of susceptibility is determined by the ending parts. The full four vertex is a solution of the Bethe-Salpeter equation

$$D = \text{diagram} - \text{diagram with } D, \quad (2.8)$$

with irreducible four vertex D that, in a same way as self-energy, describes scattering processes originated from local correlations and cannot be divided into parts by cutting off two zero-order Green's function lines.

B. Strong-coupling approach

On the other hand, an alternative approach based on the expansion over electron hopping around the strong-coupling limit can be built [9,10]. In this case, the single-electron Green's functions are determined by the Larkin equation [9,10]

$$G_{\sigma\mathbf{k}}(\omega_\nu) \equiv \text{diagram} = \text{diagram} + \text{diagram} \quad (2.9)$$

or

$$G_{\sigma\mathbf{k}}(\omega_\nu) = \Xi_{\sigma\mathbf{k}}(\omega_\nu) + \Xi_{\sigma\mathbf{k}}(\omega_\nu) t_{\mathbf{k}} G_{\sigma\mathbf{k}}(\omega_\nu) \quad (2.10)$$

$$= \frac{1}{\Xi_{\sigma\mathbf{k}}^{-1}(\omega_\nu) - t_{\mathbf{k}}},$$

where $\Xi_{\sigma\mathbf{k}}(\omega_\nu)$ is an irreducible according to Larkin part which cannot be divided into parts by cutting off one hopping (wavy) line.

Now, susceptibilities can be presented in the following form

$$\chi_{\mathbf{q}}^{AB}(i\omega_m) = \text{diagram} - \text{diagram with } D + \text{diagram with } L, \quad (2.11)$$

where

$$\text{diagram} = \text{diagram} + \text{diagram} \quad (2.12)$$

is a sum of the chains of hopping lines and full four vertex is a solution of the equation

$$L = \text{diagram} - \text{diagram with } L, \quad (2.13)$$

In Eqs. (2.11) and (2.13) quantities diagram , diagram and L are irreducible vertices which cannot be divided into parts by cutting off two wavy (hopping) lines. It should be noted that, in contrast to the weak-coupling approach, vertices in the strong-coupling approach correspond to irreducible many-particle Green's functions.

C. Connection between approaches

From Eqs. (2.5) and (2.10) one can get a connection between the self-energy and the irreducible vertex function according to the Larkin equation:

$$\Xi_{\sigma\mathbf{k}}^{-1}(i\omega_\nu) = i\omega_\nu + \mu - \Sigma_{\sigma\mathbf{k}}(i\omega_\nu). \quad (2.14)$$

The connection between the four vertices in the weak and strong coupling approaches is more complicated. For the full four vertices one can get

$$L = \text{diagram} - \text{diagram with } D, \quad (2.15)$$

whereas the irreducible four vertices are connected by equation

$$D = \text{diagram} - \text{diagram with } D', \quad (2.16)$$

where D' is a solution of equation

$$D' = \text{diagram} - \text{diagram with } D'. \quad (2.17)$$

Here

$$\text{diagram} = \text{diagram} + \text{diagram} + \text{diagram} = \text{diagram} - \text{diagram} - \text{diagram} \quad (2.18)$$

In the case when the operators \hat{A} and \hat{B} are constructed only by the electronic operators, then for three and two vertices we find

$$\text{diagram} = \text{diagram} - \text{diagram with } D', \quad (2.19)$$

and

$$\text{diagram} = \text{diagram with } D' - \text{diagram} \quad (2.20)$$

which can be treated as some kind of sum rules.

III. DYNAMICAL MEAN FIELD THEORY

In the case of infinite dimensions $d \rightarrow \infty$ one should scale the hopping integral according to

$$t_{ij} \rightarrow \frac{t_{ij}}{\sqrt{d}} \quad (3.1)$$

in order to obtain a finite density-of-states and it was shown by Metzner [3] that in this limit the irreducible part becomes local

$$\Xi_{ij\sigma}(\tau - \tau') = \delta_{ij} \Xi_{\sigma}(\tau - \tau') \quad (3.2)$$

or

$$\Xi_{\sigma\mathbf{k}}(\omega_{\nu}) = \Xi_{\sigma}(\omega_{\nu}). \quad (3.3)$$

Such a site-diagonal function, as it was shown by Brandt and Mielsch [6], can be calculated by mapping the $d \rightarrow \infty$ lattice problem (2.1) with intersite hopping (3.1) onto the atomic model with single-site hopping

$$H_t \rightarrow \int_0^{\beta} d\tau \int_0^{\beta} d\tau' \sum_{\sigma} \zeta_{\sigma}(\tau - \tau') a_{\sigma}^{\dagger}(\tau) a_{\sigma}(\tau'). \quad (3.4)$$

Here $\zeta_{\sigma}(\tau - \tau')$ is the auxiliary Kadanoff-Baym field (dynamical mean field) which has to be self-consistently determined from the condition that the same function $\Xi_{\sigma}(\omega_{\nu})$ defines the Green's function for the lattice and atomic model. The self-consistent set of equations for $\Xi_{\sigma}(\omega_{\nu})$ and $\zeta_{\sigma}(\omega_{\nu})$ (e. g., see Ref. [1] and references therein) is the following:

$$\frac{1}{N} \sum_{\mathbf{k}} \frac{1}{\Xi_{\sigma}^{-1}(\omega_{\nu}) - t_{\mathbf{k}}} = \frac{1}{\Xi_{\sigma}^{-1}(\omega_{\nu}) - \zeta_{\sigma}(\omega_{\nu})} \quad (3.5)$$

$$= G_{\sigma}^{(a)}(\omega_{\nu}, \{\zeta_{\sigma}(\omega_{\nu})\}),$$

where $G_{\sigma}^{(a)}(\omega_{\nu}, \{\zeta_{\sigma}(\omega_{\nu})\})$ is the Green's function for the atomic model (3.4).

In the same way as it was done by Metzner [3] for the irreducible part $\Xi_{\sigma}(\omega_{\nu})$ one can prove that in the $d \rightarrow \infty$ limit all irreducible vertices in the strong-coupling approach (Eqs. (2.11) and (2.13)) are also single site quantities. So, they can be also be calculated from the atomic model. On the other hand, using Eqs. (2.14)–(2.20) it is easy to show that the self-energy and irreducible vertices in the weak-coupling approach are also local quantities (in Refs. [5] that was proved using a different approach).

In order to calculate these single-site irreducible vertices first of all one has to calculate an irreducible many particle Green's functions for atomic model (3.4), i. e.,

$$\begin{aligned} \textcircled{1} &\equiv \langle T a_1^{\dagger} a_2 a_3^{\dagger} a_4 \rangle_a \\ &- \langle T a_1^{\dagger} a_2 \rangle_a \langle T a_3^{\dagger} a_4 \rangle_a + \langle T a_1^{\dagger} a_4 \rangle_a \langle T a_3^{\dagger} a_2 \rangle_a, \end{aligned} \quad (3.6)$$

$$\textcircled{1} &\equiv \langle T \hat{A}_0 a_1^{\dagger} a_2 \rangle_a - \langle \hat{A}_0 \rangle_a \langle T a_1^{\dagger} a_2 \rangle_a \quad (3.7)$$

and

$$\textcircled{1} \equiv \langle T \hat{A}_0 \hat{B}_1 \rangle_a - \langle \hat{A}_0 \rangle_a \langle \hat{B}_1 \rangle_a. \quad (3.8)$$

Then irreducible four vertex \textcircled{D} for the weak-coupling approach can be obtained from equation (2.8), where now arrows indicate single-electron Green's functions for the atomic model (3.5) and full four vertex is determined from the many-particle Green's function by

$$\textcircled{D} = \textcircled{D}. \quad (3.9)$$

On the other hand, irreducible four vertex \textcircled{L} for the strong-coupling approach can be obtained from equation (2.13), where the full four vertex is determined from the many-particle Green's function by

$$\textcircled{L} = \textcircled{L}. \quad (3.10)$$

or

$$\textcircled{L} = \textcircled{L}. \quad (3.11)$$

Now, the thin wavy lines are the dynamical mean field $\zeta_{\sigma}(\omega_{\nu})$ and the thick ones, in contrast to (2.12), represent the sum of chains of wavy lines

$$\tilde{\zeta}_{\sigma}(\omega_{\nu}) = \frac{\zeta_{\sigma}(\omega_{\nu})}{1 - \Xi_{\sigma}(\omega_{\nu}) \zeta_{\sigma}(\omega_{\nu})} = \zeta_{\sigma}(\omega_{\nu}) \frac{G_{\sigma}^{(a)}(\omega_{\nu})}{\Xi_{\sigma}(\omega_{\nu})}. \quad (3.12)$$

From the expression for the irreducible many particle Green's function (3.7), (3.8) and (3.6) for atomic model one can find irreducible vertices \textcircled{L} and \textcircled{L} by equations

$$\textcircled{L} = \textcircled{L} - \textcircled{L}, \quad (3.13)$$

and

$$\textcircled{L} = \textcircled{L} + \textcircled{L} - \textcircled{L}, \quad (3.14)$$

respectively, that complete the calculation of the irreducible vertices for the dynamical susceptibilities.

Finally, for the lattice dynamical susceptibility in the weak (2.7) and strong (2.11) coupling approaches we get

$$- \circled{1} \left[\left(\textcircled{1} \right)^{-1} + \left(\textcircled{1} \right)^{-1} \left(\textcircled{D} \right)^{-1} - \left(\textcircled{1} \right)^{-1} \right]^{-1} \circled{1}, \quad (3.15)$$

and

$$\textcircled{1} + \left\langle \left[\left(\textcircled{1} \right)^{-1} \left(\textcircled{L} \right)^{-1} - \left(\textcircled{1} \right)^{-1} \right]^{-1} \right\rangle, \quad (3.16)$$

respectively. Here, $(\dots)^{-1}$ denote an inverse kernels of the corresponding integral equations,

$$\textcircled{1} = G_{\sigma}^{(a)}(\omega_{\nu}) G_{\sigma}^{(a)}(\omega_{\nu+m}), \quad (3.17)$$

and

$$\textcircled{1} = \frac{1}{N} \sum_{\mathbf{k}} G_{\sigma\mathbf{k}}(\omega_{\nu}) G_{\sigma\mathbf{k}+\mathbf{q}}(\omega_{\nu+m}). \quad (3.18)$$

IV. BINARY ALLOY TYPE MODELS

To test the possibilities of the above approach we consider a binary alloy type model

$$H_i = \frac{g}{2} (P_i^+ - P_i^-) n_i - \frac{h}{2} (P_i^+ - P_i^-), \quad (4.1)$$

where $P_i^\pm = \frac{1}{2} \pm S_i^z$ for the $U = 0$ pseudospin-electron (PE) model [11], $P_i^+ = c_i$, $P_i^- = 1 - c_i$ for a binary alloy, and $a_{i\sigma} \rightarrow d_i$, $n_i = d_i^\dagger d_i$, $P_i^+ = f_i^\dagger f_i$, $P_i^- = 1 - f_i^\dagger f_i$ for the Falicov-Kimball (FK) model [12]. The main difference between these models is in the way that the averaging procedure is performed (a statistical one for the PE and FK models and a configurational one for the binary alloy) and in the thermodynamical regimes ($h = \text{const}$ for the PE model, $c = \text{const}$ for the binary alloy and $n_d = \text{const}$ and/or $n_f = \text{const}$ for the FK model).

The single-particle Green's function for the effective atomic model (3.4) is a coherent sum of the Green's functions for subspaces $S_i^z = \pm \frac{1}{2}$ and is equal to (see Refs. [6,13,4])

$$G_\sigma^{(a)}(\omega_\nu) = \frac{\langle P^+ \rangle}{i\omega_\nu + \mu - \zeta_\sigma(\omega_\nu) - \frac{g}{2}} + \frac{\langle P^- \rangle}{i\omega_\nu + \mu - \zeta_\sigma(\omega_\nu) + \frac{g}{2}} \quad (4.2)$$

which allows us to find solutions of Eq. (3.5) for the irreducible part $\Xi_\sigma(\omega_\nu)$ and dynamical mean field $\zeta_\sigma(\omega_\nu)$.

The Fourier transform of the two-electron Green's function $\langle T a_1^\dagger a_2 a_3^\dagger a_4 \rangle$ is also a coherent sum of the two-electron Green's functions for subspaces

$$G_{\sigma_1 \sigma'_1}^{\sigma \sigma'} \left(\begin{array}{cc} \omega_\nu & \omega_{\nu'} \\ \omega_{\nu+m} & \omega_{\nu'+m} \end{array} \right) = \sum_{\pm} \left\{ \frac{\delta_{m0} \delta_{\sigma\sigma_1} \delta_{\sigma'\sigma'_1} \langle P^\pm \rangle}{[i\omega_\nu + \mu - \zeta_\sigma(\omega_\nu) \mp \frac{g}{2}] [i\omega_{\nu'} + \mu - \zeta_{\sigma'}(\omega_{\nu'}) \mp \frac{g}{2}]} - \frac{\delta_{\nu\nu'} \delta_{\sigma\sigma'} \delta_{\sigma_1\sigma'_1} \langle P^\pm \rangle}{[i\omega_\nu + \mu - \zeta_\sigma(\omega_\nu) \mp \frac{g}{2}] [i\omega_{\nu'+m} + \mu - \zeta_{\sigma_1}(\omega_{\nu'+m}) \mp \frac{g}{2}]} \right\} \quad (4.3)$$

that gives for the irreducible two-electron Green's function (3.6) an expression which is a sum of the two separable functions

$$\tilde{G}_{\sigma_1 \sigma'_1}^{\sigma \sigma'} \left(\begin{array}{cc} \omega_\nu & \omega_{\nu'} \\ \omega_{\nu+m} & \omega_{\nu'+m} \end{array} \right) = \delta_{m0} \delta_{\sigma\sigma_1} \delta_{\sigma'\sigma'_1} \Lambda_\sigma(\omega_\nu) \Lambda_{\sigma'}(\omega_{\nu'}) - \delta_{\nu\nu'} \delta_{\sigma\sigma'} \delta_{\sigma_1\sigma'_1} \Lambda_\sigma(\omega_\nu) \Lambda_{\sigma_1}(\omega_{\nu'+m}), \quad (4.4)$$

where

$$\Lambda_\sigma(\omega_\nu) = \frac{g \sqrt{\langle P^+ \rangle \langle P^- \rangle}}{[i\omega_\nu + \mu - \zeta_\sigma(\omega_\nu)]^2 - \frac{g^2}{4}}. \quad (4.5)$$

Such a separable form allows us to calculate the inverse kernels of the integral equations and to find all quantities in an analytical form.

Within the weak-coupling approach, starting from the expression (4.4) with the use of Eq. (3.9), one can find solution of the Bethe-Salpeter equation for the irreducible four vertex in an analytical form:

$$\Gamma_{\sigma_1 \sigma'_1}^{\sigma \sigma'} \left(\begin{array}{cc} \omega_\nu & \omega_{\nu'} \\ \omega_{\nu+m} & \omega_{\nu'+m} \end{array} \right) = \frac{\Lambda_\sigma(\omega_\nu)}{G_\sigma^2(\omega_\nu) + \Lambda_\sigma^2(\omega_\nu)} \times \frac{\delta_{m0} \delta_{\sigma\sigma_1} \delta_{\sigma'\sigma'_1}}{1 - \sum_{\nu''\sigma''} \frac{\Lambda_{\sigma''}^2(\omega_{\nu''})}{G_{\sigma''}^2(\omega_{\nu''}) + \Lambda_{\sigma''}^2(\omega_{\nu''})}} \cdot \frac{\Lambda_{\sigma'}(\omega_{\nu'})}{G_{\sigma'}^2(\omega_{\nu'}) + \Lambda_{\sigma'}^2(\omega_{\nu'})} - \frac{\delta_{\nu\nu'} \delta_{\sigma\sigma'} \delta_{\sigma_1\sigma'_1}}{G_\sigma(\omega_\nu) G_{\sigma_1}(\omega_{\nu'+m})} \times \frac{\Lambda_\sigma(\omega_\nu) \Lambda_{\sigma_1}(\omega_{\nu'+m})}{G_\sigma(\omega_\nu) G_{\sigma_1}(\omega_{\nu'+m}) + \Lambda_\sigma(\omega_\nu) \Lambda_{\sigma_1}(\omega_{\nu'+m})}, \quad (4.6)$$

which must be substituted into Eq. (2.8) for the full four vertex for lattice and allows to calculate electron susceptibilities, e. g., for charge susceptibility one can get

$$\chi_{\mathbf{q}}^{nn}(\omega_m) = \delta_{m0} \frac{\Delta_n^2}{T - \Theta(T, \mathbf{q})} + K_{\mathbf{q}}^{nn}(\omega_m), \quad (4.7)$$

$$K_{\mathbf{q}}^{nn}(\omega_m) = \frac{1}{\beta} \sum_{\nu\sigma} \frac{1}{\chi_{\sigma\mathbf{q}}^{-1}(\omega_\nu, \omega_m) - \Gamma_\sigma(\omega_\nu, \omega_m)}, \quad (4.8)$$

where

$$\Gamma_\sigma(\omega_\nu, \omega_m) = \frac{\Lambda_\sigma(\omega_\nu) \Lambda_\sigma(\omega_{\nu+m})}{\tilde{\chi}_\sigma(\omega_\nu, \omega_m) [\Lambda_\sigma(\omega_\nu) \Lambda_\sigma(\omega_{\nu+m}) - \tilde{\chi}_\sigma(\omega_\nu, \omega_m)]} \quad (4.9)$$

originates from the last term in (4.6) and

$$\Delta_n = \frac{1}{\beta} \sum_{\nu\sigma} \frac{\Lambda_\sigma(\omega_\nu) \tilde{\chi}_\sigma(\omega_\nu, 0) \chi_{\sigma\mathbf{q}}(\omega_\nu, 0)}{\tilde{\chi}_\sigma^2(\omega_\nu, 0) + \Lambda_\sigma^2(\omega_\nu) [\chi_{\sigma\mathbf{q}}(\omega_\nu, 0) - \tilde{\chi}_\sigma(\omega_\nu, 0)]}, \quad (4.10)$$

$$\Theta(T, \mathbf{q}) = \frac{1}{\beta} \sum_{\nu\sigma} \frac{\Lambda_\sigma^2(\omega_\nu) [\chi_{\sigma\mathbf{q}}(\omega_\nu, 0) - \tilde{\chi}_\sigma(\omega_\nu, 0)]}{\tilde{\chi}_\sigma^2(\omega_\nu, 0) + \Lambda_\sigma^2(\omega_\nu) [\chi_{\sigma\mathbf{q}}(\omega_\nu, 0) - \tilde{\chi}_\sigma(\omega_\nu, 0)]}, \quad (4.11)$$

$$\chi_{\sigma\mathbf{q}}(\omega_\nu, \omega_m) = -\frac{1}{N} \sum_{\mathbf{k}} G_{\sigma\mathbf{k}}(\omega_\nu) G_{\sigma\mathbf{k}+\mathbf{q}}(\omega_{\nu+m}), \quad (4.12)$$

$$\tilde{\chi}_\sigma(\omega_\nu, \omega_m) = -G_\sigma^{(a)}(\omega_\nu) G_\sigma^{(a)}(\omega_{\nu+m}). \quad (4.13)$$

But such a diagrammatic weak-coupling approach does not allow one to calculate pseudospin and mixed susceptibilities.

On the other hand, the strong-coupling approach allows us to calculate all susceptibilities. To do this, we calculate the irreducible many-particle Green's functions

$$\left\langle T n_\sigma(\tau) a_{\sigma'}^\dagger(\tau') a_{\sigma'}(\tau'') \right\rangle_{\text{irr}} \rightarrow \delta_{m0} \sum_{\nu'} \Lambda_\sigma(\omega_{\nu'}) \Lambda_{\sigma'}(\omega_\nu) - \delta_{\sigma\sigma'} \left[\Lambda_\sigma(\omega_\nu) \Lambda_{\sigma'}(\omega_{\nu+m}) + G_\sigma^{(a)}(\omega_\nu) G_{\sigma'}^{(a)}(\omega_{\nu+m}) \right], \quad (4.14)$$

$$\langle TS^z(\tau)a_\sigma^\dagger(\tau')a_\sigma(\tau'') \rangle_{\text{irr}} \rightarrow \delta_{m0} \sqrt{\langle P^+ \rangle \langle P^- \rangle} \Lambda_\sigma(\omega_\nu), \quad (4.15)$$

$$\langle TS^z(\tau)S^z(\tau') \rangle_{\text{irr}} \rightarrow \delta_{m0} \langle P^+ \rangle \langle P^- \rangle, \quad (4.16)$$

$$\langle Tn_\sigma(\tau)n_{\sigma'}(\tau') \rangle_{\text{irr}} \rightarrow \delta_{m0} \sum_\nu \Lambda_\sigma(\omega_\nu) \sum_{\nu'} \Lambda_{\sigma'}(\omega_{\nu'}) - \delta_{\sigma\sigma'} \sum_\nu \left[\Lambda_\sigma(\omega_\nu) \Lambda_\sigma(\omega_{\nu+m}) + G_\sigma^{(a)}(\omega_\nu) G_\sigma^{(a)}(\omega_{\nu+m}) \right] \quad (4.17)$$

$$\langle TS^z(\tau)n_\sigma(\tau') \rangle_{\text{irr}} \rightarrow \delta_{m0} \sqrt{\langle P^+ \rangle \langle P^- \rangle} \sum_\nu \Lambda_\sigma(\omega_\nu), \quad (4.18)$$

After substituting (4.14)–(4.18) into Eq. (3.16) we get for the charge susceptibility the same expression (4.7), whereas for the pseudospin and mixed susceptibilities

$$\chi_{\mathbf{q}}^{S^z S^z}(\omega_m) = \delta_{m0} \frac{\Delta_{S^z}^2}{T - \Theta(T, \mathbf{q})} = \delta_{m0} \frac{\langle P^+ \rangle \langle P^- \rangle}{T - \Theta(T, \mathbf{q})}, \quad (4.19)$$

$$\chi_{\mathbf{q}}^{n S^z}(\omega_m) = \chi_{\mathbf{q}}^{S^z n}(\omega_m) = \delta_{m0} \frac{\Delta_{S^z} \Delta_n}{T - \Theta(T, \mathbf{q})}, \quad (4.20)$$

where

$$\Delta_{S^z} = \sqrt{\langle P^+ \rangle \langle P^- \rangle}. \quad (4.21)$$

Expression (4.11) for $\Theta(T, \mathbf{q})$ coincides with the one obtained by Freericks [7] from the equations for the static susceptibilities ($\omega_m = 0$) derived by Brandt and Mielsch [6]. The irreducible four vertex (4.9) was also derived by Freericks and Miller [14] within the Baym–Kadanoff formalism and used to find the exact solution for the nonresonant Raman scattering for the FK model [15,16].

V. DISCUSSION

For the binary alloy (Falikov–Kimball) model (4.1) expressions (4.7), (4.19) and (4.20) define the so-called isothermal susceptibilities [17]. Furthermore, the pseudospin (4.19) and mixed (4.20) susceptibilities are only static (with factor δ_{m0}) because the pseudospin operator S_i^z commutes with the Hamiltonian and is an integral of motion. It should be noted, that the binary alloy model (4.1) can be reduced to the Ising type model with an effective multisite retarded pseudospin interactions by taking a trace of the statistical operator with the Hamiltonian (4.1) over electron (fermion) variables [4]. This explains the Ising type expression obtained for the pseudospin susceptibility (4.19), but now the expression for the critical temperature $\Theta(T, \mathbf{q})$ is more complicated.

The expression for the charge susceptibility (4.7) contains two terms. The first one is static and can be written as

$$\chi^{n S^z} \left[\chi^{S^z S^z} \right]^{-1} \chi^{S^z n}. \quad (5.1)$$

This describes the contribution from the pseudospin subsystem to the charge susceptibility. It gives the main contribution to the static susceptibilities. The second term $K_{\mathbf{q}}^{nn}(\omega_m)$ in (4.7) gives the pure electron response and describes the so-called isolated (Kubo) susceptibility [17]. In general, terms with the factor δ_{m0} give the difference between the isothermal and isolated susceptibilities (see Appendix in Ref. [18]).

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A. M. SHVAIKA

**ДИНАМІЧНІ СПРИЙНЯТЛИВОСТІ В ПІДХОДІ СИЛЬНОГО ЗВ'ЯЗКУ:
ЗАГАЛЬНА СХЕМА ТА МОДЕЛЬ ФАЛІКОВА–КІМБАЛА**

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У межах теорії динамічного середнього поля розвинена загальна схема до розрахунку динамічних сприйнятливостей сильнокорельованих електронних систем. Підхід ґрунтується на розвиненнях за електронним переносом щодо атомної межі (у межах діаграмної техніки для вузлових операторів: проєкційних чи Габбарда) для безмежної розмірності простору. Як приклад розглянуто моделі Фалікова–Кімбала та спрощену псевдоспін-електронну, для яких отримано аналітичні вирази для динамічних сприйнятливостей.